Equation 2 is still three dimensional with three independent diffusion constants,  $D_1$ ,  $D_2$  and  $D_3$  corresponding to the three crystalline axes. However, if the material has cubic symmetry, it can be shown that the bulk diffusion is isotropic; that is, independent of crystalline direction with  $D_1=D_2=D_3=D$  where D is called the diffusion constant. If the geometry is such that the concentration is a function only of a single cartesian coordinate and time, equation 2 reduces to the usual one dimensional diffusion equation:

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$$
(3)

Solutions of equation 3 for various initial conditions are tabulated and discussed by Crank.<sup>14</sup> The solution for a semi-infinite rod with a delta function source on the end is given by equation 4:

$$C = \frac{\alpha}{2(100T)} e \times p\left(\frac{-\chi^2}{40t}\right)$$
(4)

where  $\propto$  is a constant associated with the strength of the source, t is the anneal time at constant pressure and temperature, and x is the penetration distance measured from the source. A rule of thumb for determining the length of rod needed in order for equation 4 to be a good approximation for the solution of the diffusion equation for a finite rod is  $\ell > 2 \sqrt{Dt}$ .

If we take the log of both sides of equation 4,

$$\ln C = \frac{-X^2}{40t} + \ln\left(\frac{\alpha}{2\sqrt{\pi}Dt'}\right) \tag{5}$$

we see that -1/4Dt is the slope of the log of the concentration vs the square of the penetration distance curve.

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